FIELD TEST VALIDATION OF THE DEGADIS MODEL

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Summary

An interactive computer model (DEGADIS) which uses a lumped parameter approach to simulate a wide variety of denser-than-air gas release scenarios, including instantaneous releases, time-varying releases, and continuous releases on a flat, obstacle-free surface is briefly described. The model accounts for negative buoyancy-induced and stably stratified shear flows and is consistent with the limiting passive dispersion characteristics of demonstrated air pollution models.

Predicted maximum concentration as a function of distance is compared to the maximum reported concentration for field scale releases of liquefied natural gas (LNG), liquefied petroleum gas (LPG as propane), and Freon-12/nitrogen mixtures from the Burro/Coyote, Maplin Sands, and Thorney Island Phase I trials, respectively. From these, the variability of the distance realized to a concentration level of 5, 2.5, and 1% for a given release is quantified based on the predicted distance. Comparisons of observed and model-predicted dispersion of nitrogen tetroxide from a large scale field test program (the U.S. Air Force Eagle series) are also presented.

1. Introduction

Consider a ground-level release of a mass of denser-than-air gas (DTAG) on flat, obstacle-free terrain. The initial gas cloud may result directly from (1) an aboveground release such as a release of pressurized gases, as in a chlorine tank rupture, or (2) indirectly from a ground-level source such as the evaporation of a released liquid as in the case of a spill onto the sea of liquefied petroleum gas (LPG) or natural gas (LNG). The cloud may be initially formed as a mixture of gas or gas-liquid aerosol and (humid) air. In general, such a release would be expected to pass through three phases: (1) negative buoyancy-dominated dispersion, (2) passive dispersion, and (3) stably stratified shear flow.

1.1 Negative buoyancy-dominated dispersion phase

Rapid release of a DTAG may result in an initial cloud having similar vertical and horizontal dimensions. The initial behavior of such "compact clouds" [1] is controlled by the negative buoyancy-driven flow. The gravity-driven flow results in large scale turbulent structures which cause the cloud to dilute

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[2-6]. Since this initial turbulent motion can result in dilution by a factor larger than ten, it must be accounted for in predictions of DTAG dispersion, particularly for hydrocarbons. (Gas-air mixture flammability levels for hydrocarbons are generally O (1%).)

1.2 Passive dispersion phase

At some distance from the source, the released gas will be sufficiently dilute to justify its consideration as a trace material, and the dispersion can be modeled using approaches developed for atmospheric pollutant dispersion [7,8]. The Gaussian plume model is applicable to atmospheric dispersion problems when the dispersion of the contaminant is only a function of the atmospheric turbulence and the plume does not perturb the ambient flow field. The steadystate Gaussian plume model for ground-level releases is

$$y_{v} = \frac{Q}{\pi \sigma_{y} \sigma_{z} u} \exp\left[-\left(\frac{y}{\sqrt{2} \sigma_{y}}\right)^{2} - \left(\frac{z}{\sqrt{2} \sigma_{z}}\right)^{2}\right]$$
(1)

where σ_y and σ_z determine the shape of the Gaussian profile. Prescriptions for σ_y and σ_z as a function of distance are given by Hanna et al. [7] and Pasquill and Smith [8].

1.3 Stably stratified shear flow phase

The distinguishing feature of a neutrally buoyant plume described above is the assumption that the mean flow field is not affected by the contaminant. This is in direct contrast to the negative buoyancy-dominated flow phase where the distinguishing feature is the essentially complete determination of the mean flow field by the contaminant release as described above. An intermediate phase of the dispersion process is characterized by its similarity to a wide variety of naturally occurring flow processes in which a stably stratified plume is embedded in a turbulent mean flow. Such plumes are expected to differ importantly from neutrally buoyant plumes.

- 1. A lateral (crosswind) gravity-driven mean flow will persist until the negative buoyancy of the cloud has been reduced (by air entrainment).
- 2. Because the ratio of width to depth for these plumes is characteristically large, dilution occurs primarily as a result of vertical mixing.
- 3. The density stratification at the upper plume boundary should act to damp turbulent mixing and consequently reduce vertical mixing (air entrainment).

Fluid mixing across the density interface which characterizes a dense plume embedded in a turbulent boundary layer was reviewed by Turner [9]. There is general agreement that entrainment across such plume boundaries is correlated with a bulk Richardson number $(Ri_*=g\Delta' H/u_*^2)$. McQuaid [10], Kantha et al. [11], and Lofquist [12] have reported experimental studies from

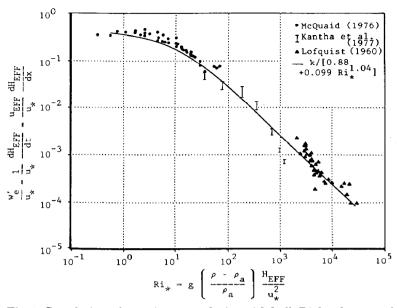


Fig. 1. Correlation of entrainment velocity with bulk Richardson number.

which entrainment velocity correlations can be derived for Richardson numbers encompassing the range of interest for DTAG dispersion.

The combined data of McQuaid, Kantha et al., and Lofquist shown in Fig. 1 were curve-fitted to give

$$w'_{e}/u_{*} = k/(0.88 + 0.099 Ri^{1.04}_{*})$$
⁽²⁾

The limiting value $(Ri_*=0)$ of $w'_e/u_*=k/0.88$ incorporates the ratio of eddy diffusivities for heat and momentum (K_H/K_M) , along with k=0.35 (as determined by Businger et al. [13] from measurements in the neutral atmospheric surface stress layer). The effect of vertical density stratification on vertical mixing shown by the data is consistent with a passive limit for w'_e/u_* of 0.4 as suggested by the solution of the diffusion equation with a constant wind velocity and mass diffusivity given by

$$K_{\rm c} = k u_* z \tag{3}$$

(which is consistent with the Gaussian plume model of eqn. 1). Furthermore, the dependence of w'_{e} on Ri_{*} for large Ri_{*} approaches

$$w'_{e} \propto Ri^{-1}_{*} \tag{4}$$

as suggested from dimensional reasoning by Turner [9].

2. The DEGADIS model

DEGADIS [14] is an adaptation of the Shell HEGADAS model described by Colenbrander [15] and Colenbrander and Puttock [16]; DEGADIS also incorporates some techniques used by van Ulden [17]. The near-field, buoyancy-dominated regime is modeled using a lumped parameter model of a DTAG "secondary source" cloud which incorporates air entrainment at the gravityspreading front using a frontal entrainment velocity. The downwind dispersion phase assumes a power law concentration distribution in the vertical direction and a modified Gaussian profile in the horizontal direction with a power law specification for the wind profile (Fig. 2). The source model represents a spatially averaged concentration of gas present over the primary source, while the downwind dispersion phase of the calculation models an ensemble average of the concentration downwind of the source.

For the negative buoyancy-dominated dispersion phase, the model is based on laboratory-scale releases of a DTAG in a calm environment [5,6]. For the stably stratified shear flow phase, the model is based on the laboratory-scale experiments of McQuaid [10], Kantha et al. [11] and Lofquist [12] discussed in Section 1.3. Established passive atmospheric dispersion modeling principles are used for the passive dispersion phase. It is emphasized that DEGADIS was not calibrated to any DTAG field-scale tests. A complete description of the DEGADIS model is included in Havens and Spicer [14].

3. Analysis and simulation of selected field experiments

The DEGADIS model has been used to simulate a large collection of field experimental DTAG releases (Table 1). The field tests simulated include small continuous LPG releases (order 0.1 to 1.0 kg/s) on land from diked sources, continuous LPG and LNG releases onto water with release rates of the order 10–100 kg/s, instantaneous releases of LNG onto water of approximately 5000 kg, instantaneous releases of Freon-12/nitrogen mixtures of approximately 5000 kg on land, and quasi-steady releases of nitrogen tetroxide (N₂O₄). The meteorological conditions in the experimental releases include wind speeds of approximately 1.0–10.0 m/s, relative humidity from essentially zero to about 85%, and atmospheric stabilities ranging from Pasquill B to E. In general, the field tests of Table 1 were directed toward either hydrocarbon flammability levels (O(1%)) or toxic gas levels (O(100 ppm)). (A complete summary of simulated releases can be found in Havens and Spicer [14] and Spicer and Havens [18].)

3.1 Hydrocarbon flammability levels — O(1%)

All of the field scale experimental programs in Table 1 except the USAF Eagle series were directed to measuring concentrations no lower than O(0.1%).

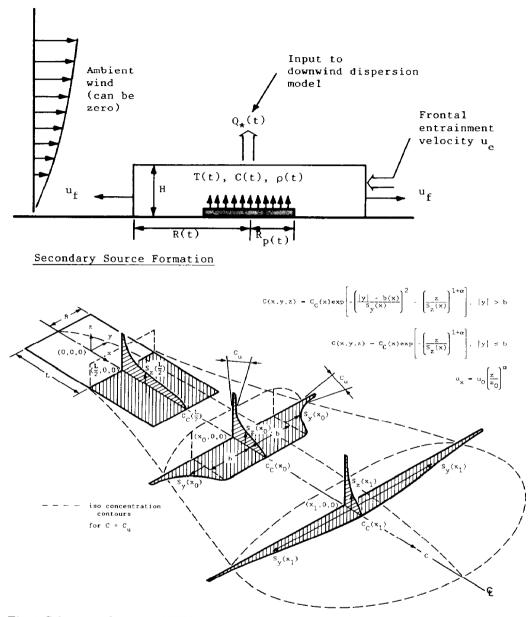


Fig. 2. Schematic diagram of DEGADIS denser-than-air gas dispersion model.

In the U.S. DOE releases reported by Welker [19], propane was released into concrete-lined pits nominally 1.5, 3, and 6 meters square. Peak (or maximum reported) and mean concentrations were reported at ground level at positions estimated to be in the plume centerline. Figure 3 is a typical compar-

TABLE 1

Test series	Material released	Release type/size	Wind speed range (m/s)	Pasquill stability range	Release Richardson number ^a
British Health & Safety Executive, Thorney Island	Freon-12/ nitrogen mixtures	Instantaneous, 3500-4800 kg	1.7-7.5	C-E	_
Shell Research, Maplin Sands	LNG and LPG ^b	Steady state, 17.7–41.7 kg/s	4.1-9.8	D	4-100
USAF Eagle series releases	Nitrogen tetroxide	Steady state, 1.6–3.0 kg/s	3.7-5.6	D	4-40
U.S. DOE Burro, Coyote series releases	LNG and LPG ^b	Continuous, time-limited, $9.7-16.7 \times 10^3$ kg	2.4-11.9	C-E	4.7-9 30
U.S. DOE releases by Welker	LPG⁵	Steady state, 0.019-0.55 kg/s	2.0-7.5	B-D	0.1-3.5

Summary of field experimental DTAG releases

"The continuous release Richardson number is defined by

$$Ri_{\rm c} = \frac{g}{u_*^2} \left[\frac{\rho_{\rm i} - \rho_{\rm a}}{\rho_{\rm a}} \right] \left[\frac{\dot{m}}{\rho_{\rm i} uD} \right]$$

where \dot{m} is the contaminant evolution rate (kg/s), u is the ambient wind velocity (m/s) specified at an (arbitrary) height, and D is the source diameter. Ri_c represents a ratio of the potential energy characteristic of the release to a measure of the ambient turbulent kinetic energy. Three ranges of Ri_c are important: $Ri_c < 1$ release is passive from the source; $1 \leq Ri_c \leq 32$ release is in the stably stratified shear flow phase; $Ri_c > 32$ release is in the negative buoyancy-dominated dispersion phase. The Thorney Island trials release Richardson numbers were not calculated since these are instantaneous releases.

^bLPG was predominantly propane.

ison of the reported centerline concentrations to the DEGADIS-predicted maximum centerline concentration. Welker showed the reported centerline concentrations to be described reasonably well by a passive dispersion model in agreement with the release Richardson number range in Table 1.

In contrast to the small release Richardson numbers of the releases reported by Welker, the British Helath and Safety Executive releases at Thorney Island were instantaneous releases of nominal 2000 m³ volumes of Freon-12/nitrogen mixtures [20]. Figure 4 is a typical comparison of the maximum reported concentration to the DEGADIS-predicted maximum centerline concentration.

The U.S. DOE Burro and Coyote series releases were performed by Law-

TEST: Welker 275-1

Source Description

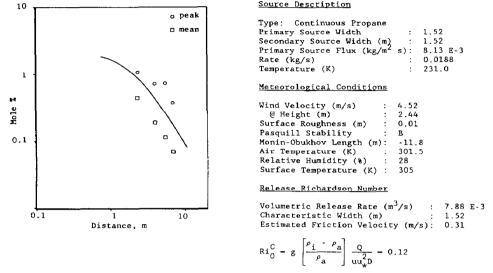


Fig. 3. DEGADIS-predicted centerline maximum concentration and reported concentration vs. distance — Welker 275-1.

TEST: Thorney 15

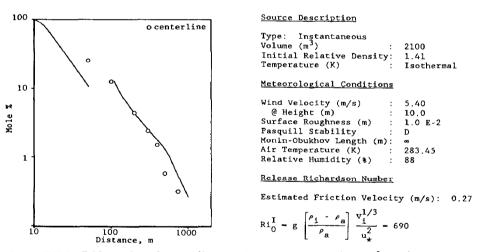


Fig. 4. DEGADIS-predicted centerline maximum concentration and maximum reported concentration vs. distance — Thorney 15.

rence Livermore National Laboratories (LLNL) at China Lake, California [21]. LNG was released on water with subsequent dispersion over land. Figure 5 shows a typical comparison of the DEGADIS-predicted maximum centerline TEST: Burro 8

Source Description

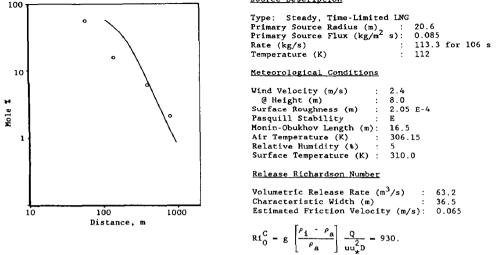


Fig. 5. DEGADIS-predicted centerline maximum concentration and maximum reported concentration vs. distance — Burro 8.

TEST: Maplin 46

Source Description

Meteorological Conditions

8.49 0.12 231.0

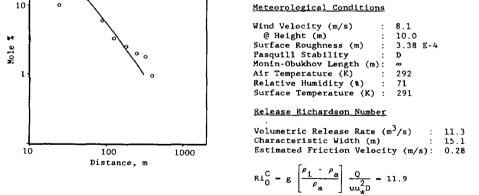


Fig. 6. DEGADIS-predicted centerline maximum concentration and maximum reported concentration vs. distance - Maplin 46.

100

concentration with the reported maximum concentration. The release Richardson number for these tests indicates the importance of the negative buoyancy-dominated dispersion phase and the stably stratified shear flow phase.

The Shell Research releases at Maplin Sands were a series of LNG and LPG (propane) releases on water [22]. Most of the releases were steady state. Two instantaneous releases each of LNG and LPG were reported. Figure 6 shows a typical comparison of the maximum reported (steady) concentrations to the DEGADIS-predicted maximum centerline concentration. As in the Burro and Coyote tests, the release Richardson number indicates the importance of the negative buoyancy-dominated dispersion phase and the stably stratified shear flow phase.

In order to quantify the uncertainty associated with predicted distances to concentrations of order 1%, predicted and "observed" distances to the 5%, 2.5%, and 1% concentration levels were compared. The "observed" values were determined from maximum reported concentrations for each experiment by drawing a visual best-fit straight line through the reported points in the concentration range of interest; all of the measurements used were made at heights at or below 1 m. The predicted distance to a given concentration level was based on the ground level centerline concentration calculated by DEGADIS; for the concentrations and conditions of interest, the predicted concentration level is essentially constant for heights below 1 m. From these values, a ratio of the "observed" to the predicted distance for each experiment was calculated. For this analysis, the ratio $(OBS/PRE)_y$ is assumed to be independent of the release conditions.

Table 2 includes values of the ratios (OBS/PRE)_y along with 90% confidence intervals for the average of ($\overline{OBS/PRE}$)_y for each test series and for all of the experiments together. (For instance, the Maplin Sands comparisons indicate the average ratio of the "observed" to the predicted distance to the 2.5% concentration level would be between 0.91 and 1.20 in nine out of ten realizations.) For all of the comparisons in Table 2, the 90% confidence interval for the average ratio of "observed" distance to predicted distance for a given concentration level ranged from 0.73 to 0.96 for the 5% level; for the 2.5% level, a 90% confidence interval for ($\overline{OBS/PRE}$)_{2.5} ranged from 0.82 to 1.03; for the 1% level, a 90% confidence interval for ($\overline{OBS/PRE}$)_{2.5} ranged from 0.95 to 1.24. The confidence intervals of the ratio ($\overline{OBS/PRE}$)_y can now be used to predict the range of the average distance to a given concentration level as a given concentration level so the ratio ($\overline{OBS/PRE}$)_y can now be used to predict the range of the average distance to a given concentration level as the ratio ($\overline{OBS/PRE}$)_y can now be used to predict the range of the average distance to a given concentration level under a given set of release conditions.

3.2 Toxic gas levels — O(100 ppm)

In 1983, Lawrence Livermore National Laboratories (LLNL) conducted a series of nitrogen tetroxide (N_2O_4) releases for the U.S. Air Force at the U.S. DOE Nevada Test Site (NTS). Two of these releases, Eagle 3 and 6, provided sufficient data for comparison and assessment of atmospheric gas dispersion

TABLE 2

 $Comparison \ between \ ``observed" \ and \ DEGADIS-predicted \ maximum \ distance \ to \ gas \ concentrations in the flammable \ concentration \ range$

	Ratio of "observed" distance to DEGADIS-predicted distance $(OBS/PRE)_y$ for the concentration level y:		
	y=5%	y=2.5%	y=1%
Thorney Island			
7	1.17	1.12	0.63
8	1.09	0.90	0.66
9	1.00	0.95	1.28
11	0.55	0.61	0.63
13	0.70	0.70	0.70
15	1.05	0.90	0.77
Thorney Island	0.71≤	0.70 ≤	0.64≤
90% confidence interval	$(\overline{OBS/PRE})_5 \leq 1.11$	$(\overline{OBS/PRE})_{2.5} \leq 1.02$	$(\overline{OBS/PRE})_1 \leq 0.99$
Maplin			
22	0.47	0.64	1.15
27	0.95	1.10	1.46
29	0.89	0.96	1.20
34	1.28	1.38	1.76
35	1.28	1.59	2.61
39	0.46	0.63	1.21
43	0.73	0.84	0.91
46	1.09	1.17	1.33
47	0.77	0.92	1.06
49	1.27	1.35	1.46
45 50	0.92	0.90	1.26
50 54	1.12		
54 56	0.93	1.21	1.19
		0.92	1.02
Maplin	0.80 ≤	0. <u>91≤</u>	1 <u>.15</u> ≤
90% confidence interval	$(OBS/PRE)_5 \leq 1.10$	$(\overline{\text{OBS/PRE}})_{2.5} \leq 1.20$	$(\overline{OBS/PRE})_1 \leq 1.47$
Burro			, ····
3	0.52	0.69	0.83
7	0.63	0.74	0.95
8	0.93	1.21	1.66
9	0.51	0.78	1.22
Coyote			
5	0.75	0.71	0.71
ő	0.38	0.38	0.43
Burro/Coyote	0.46≤	0.55 ≤	0.63≤
90% confidence	$(\overline{OBS/PRE})_5 0.78$	$(\overline{OBS/PRE})_{2.5} \leq 0.98$	$(OBS/PRE)_1 \leq 1.31$
interval	(ODS/1 RE)50.10	(ODS/1 RE/2.5 ≈ 0.30	$(ODS/1 RE)_1 \leq 1.31$
Summary	$0.73 \leq (OPS/DPF) < 0.06$	$0.82 \leq (OPE(DPE)) \leq 1.02$	0. <u>95</u> ≤ (OPS(PDF)) <1.94
90% confidence interval	$(OBS/PRE)_5 \leq 0.96$	(OBS/PRE) _{2.5} ≤1.03	$(OBS/PRE)_1 \leq 1.24$

TABLE 3

Comparison of Eagle 3 and Eagle 6 test results and gas dispersion model predictions [18]	
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	Maximum NO2 concentration range (ppm) ^a	σ_y (m)	σ_z (m)	
Eagle 3				
Test results	500-1040	35	3.8	
Gaussian plume	68-73	60.5	31.9	
DEGADIS	880-1170	$57.6 - 60.7^{b}$	3.2-4.1°	
Eagle 6				
Test results	160-34 0	35	7.6	
Gaussian plume	25-27	60.5	31.9	
DEGADIS	190-220	$55.6 - 56.6^{b}$	6.4–6.9 ^c	

^aThe concentration range for the model predictions are for the estimated source mass evolution rate range.

^bCalculated as $S_y/\sqrt{2}$.

^cEstimated as S_z .

modeling techniques [23]. An array of sensors designed to measure N_2O_4 concentration, temperature, and velocity was placed 25 m downwind of the gas source to measure the mass evolution rate of the released gas. Another array of sensors designed to measure NO_2 concentration, temperature, and velocity was placed 785 m downwind of the source to measure the concentration of the gas cloud as it moved downwind after release. The Eagle series tests were complicated further by the interaction of N_2O_4 with the ambient humidity which hindered concentration measurements.

Based on the measured N_2O_4 mass rate passing the 25 m sensor array and an analysis of the reactions taking place, Spicer and Havens [18] reported N_2O_4 mass evolution rates between 2.9 and 3.1 kg/s for Eagle 3 and between 1.6 and 1.7 kg/s for Eagle 6 as well as steady-state-observed maximum concentration ranges (expressed as equivalent NO₂ concentration) for Eagle 3 and 6 as summarized in Table 3. Table 3 also includes model predictions from the Gaussian plume model and DEGADIS.

For Eagle 3 and 6, the pasive dispersion model tends to underpredict the maximum concentration because of an overprediction of the vertical mixing rate (i.e. the predicted σ_z is greater than the observed σ_z). On the other hand, DEGADIS predicts maximum centerline concentrations and similarity distribution parameters σ_y and σ_z which are consistent with the experimental data; closer agreement of DEGADIS-predicted values of σ_z with observed values of σ_z compared to the passive Gaussian plume model is attributed to correctly predicting the decreased vertical mixing rate for the initial phase of the releases. These characteristics are consistent with the release Richardson number of each release. ($Ri_c = 40$ for Eagle 3 and $Ri_c = 4$ for Eagle 6.)

Conclusions and recommendations

Based on the phenomenology of DTAG dispersion, the following phases are used to describe DTAG dispersion in the atmosphere:

- Negative buoyancy-dominated dispersion
- Stably stratified shear flow
- Passive dispersion due to atmospheric turbulence

Along with established models for passive dispersion, laboratory experimental data were used to model the other dispersion phases. Laboratory data from stratified shear flow mixing experiments have been used to model the vertical dispersion of DTAG in the atmospheric constant stress layer consistently with the limiting passive dispersion behavior of demonstrated air pollution models. DEGADIS, an interactive computer model for DTAG dispersion, accounts for the three regimes of dispersion described above and for effects due to energy exchange between the dispersing cloud and the underlying surface.

The DEGADIS model has been used to simulate a wide range of field experimental DTAG releases, including small to intermediate LPG (0.1–1 kg/s) and LNG release (1–100 kg/s) on land, large-scale releases (10–150 kg/s) of LPG and LNG on water, instantaneous releases of approximately 5000 kg Freon-/nitrogen mixtures on land, and quasi-steady state releases of N₂O₄ over land. The DEGADIS model-predicted downwind gas concentration decay has been shown consistent with the field-scale experimental data currently available.

Application of DEGADIS has been primarily directed to the prediction of concentrations in the lower flammability limit range (1-5%). Based on comparison with field data, a 90% confidence interval for the average ratio of observed to calculated distance for the 2.5% concentration level would be between 0.82 and 1.03; the 90% confidence interval for the average ratio of observed to calculated distance was between 0.73 and 0.96 for the 5% level and between 0.95 and 1.24 for the 1% level.

Application of DEGADIS to the prediction of concentration levels of interest for toxic gases (O(100 ppm)) for DTAGs is less complete. For Eagle 3 and 6, downwind concentrations and observed Gaussian equivalent concentration profiles (σ_y and σ_z) were compared to model predictions using the Gaussian plume model and DEGADIS. The Gaussian plume model generally underpredicted the concentration due to an overprediction of the vertical mixing present, while DEGADIS predictions were consistent with observed concentrations and profile parameters σ_y and σ_z as would be expected from the release Richardson number.

Acknowledgements

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List of symbols

Ь	half width of horizontally homogeneous central section of gas
-	plume (m)
С	concentration (kg/m^3)
C _c	centerline, ground-level concentration (kg/m ³)
$\check{C}_{\mathbf{E}}$	constant in density intrusion (spreading) relation
D^{-}	source diameter
g	acceleration of gravity (m/s ²)
H	height or depth of density intrusion or cloud (m)
$(H/D)_{\rm i}$	initial height-to-diameter (aspect) ratio
$H_{ m EFF}$	effective cloud depth (m)
H_{i}	initial cloud height (m)
$K_{ m c}$	vertical turbulent diffusivity, mass (m ² /s)
$K_{\rm H}$	vertical turbulent diffusivity, heat (m ² /s)
$K_{\mathbf{M}}$	vertical turbulent diffusivity, momentum (m^2/s)
k	von Karman's constant, 0.35
<i>m</i>	mass source evolution rate (kg/s)
$(OBS/PRE)_y$	ratio of "observed" distance to DEGADIS-predicted distance
	for the y concentration level
$(\overline{OBS/PRE})_y$	
0()	on the order of volumetric release rate (m ³ /s)
$\begin{array}{c} Q \\ Q_{*} \end{array}$	atmospheric takeup flux (kg/m^2s)
$R^{\mathbf{q}_{*}}$	gas source cloud radius (m)
$R_{\rm p}$	primary source radius (m)
$R_{\rm p}$ $Ri_{\rm c}$	release Richardson number for continuous releases
Ri.	Richardson number
S_{ν}	horizontal concentration scaling parameter (m)
$\vec{Ri_*}$ S_y S_z	vertical concentration scaling parameter (m)
t	time (s)
T	cloud temperature (K)
u	average wind velocity (m/s)
u_{e}	horizontal or frontal entrainment velocity (m/s)
$u_{ m EFF}$	effective cloud advection velocity (m/s)
$u_{\rm f}$	cloud front velocity (m/s)
u_x	wind velocity along x-direction (m/s)
u_0	wind velocity measured at $z = z_0$ (m/s)
u_*	friction velocity (m/s)
V_{i}	initial volume (m ³)

w'_{e}	entrainment velocity associated with $H_{ m EFF}$ (m/s)
<i>x,y,z</i>	Cartesian coordinates (m)
$\mathcal{Y}_{\mathbf{v}}$	contaminant mole fraction
z_0	reference height in wind velocity profile specification (m)
α	constant in power law wind profile
⊿′	ratio of $(\rho - \rho_a)/\rho_a$
ρ	density of gas-air mixture (kg/m ³)
ρ_{a}	ambient air density (kg/m^3)
$\rho_{\rm i}$	initial cloud density (kg/m ³)
σ_{y}	Pasquill–Gifford lateral dispersion coefficient (m)
σ_z	Pasquill-Gifford vertical dispersion coefficient (m)

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